



# Study of Inertia Weight Parameter for Boundary Element Inverse Analysis to Detect RC Corrosion

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# Corrosion of rebar

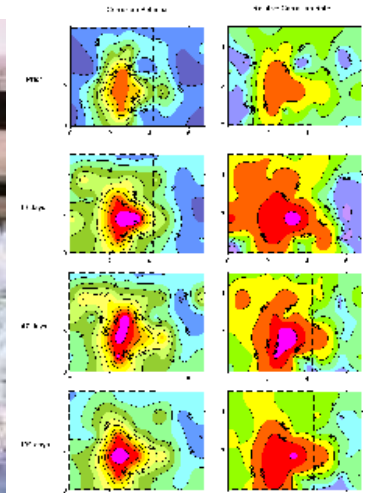


# The failures of RC structures due to corrosion

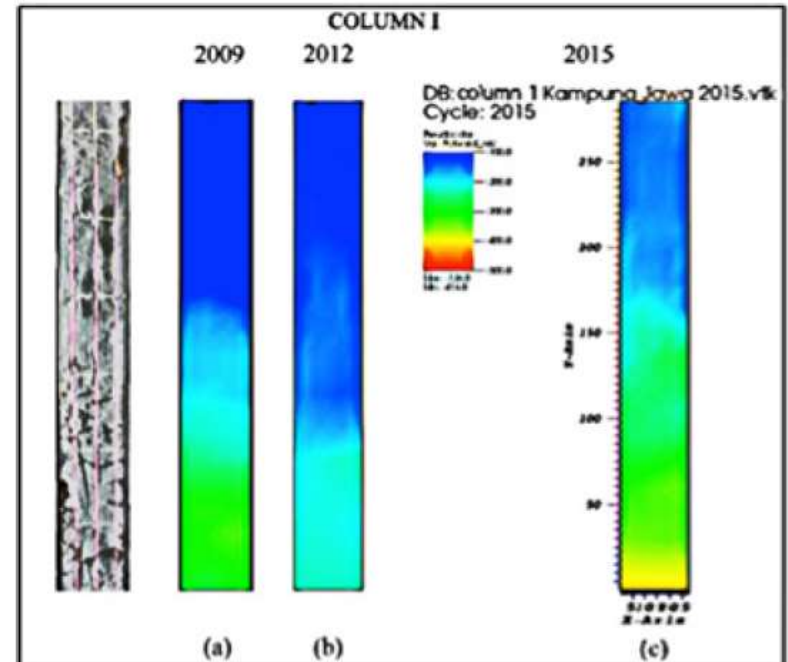
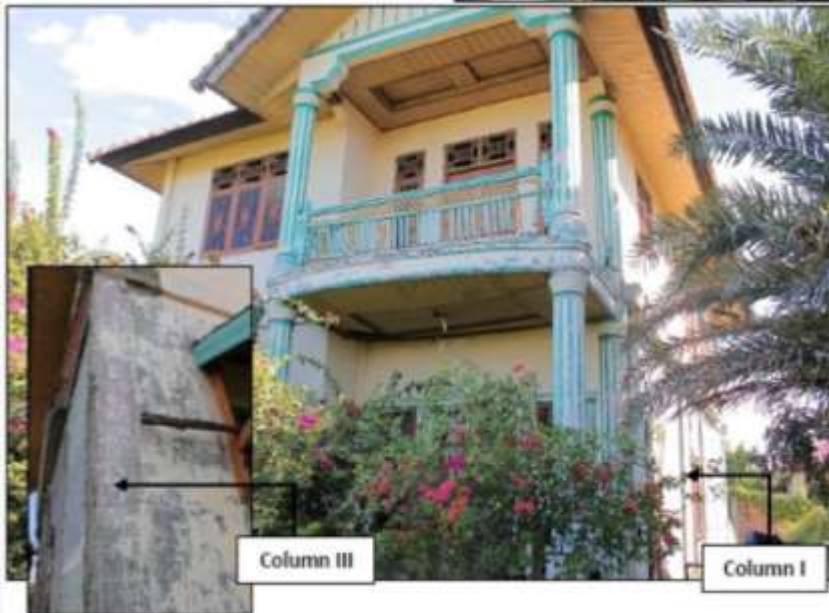


# Direct Corrosion Monitoring

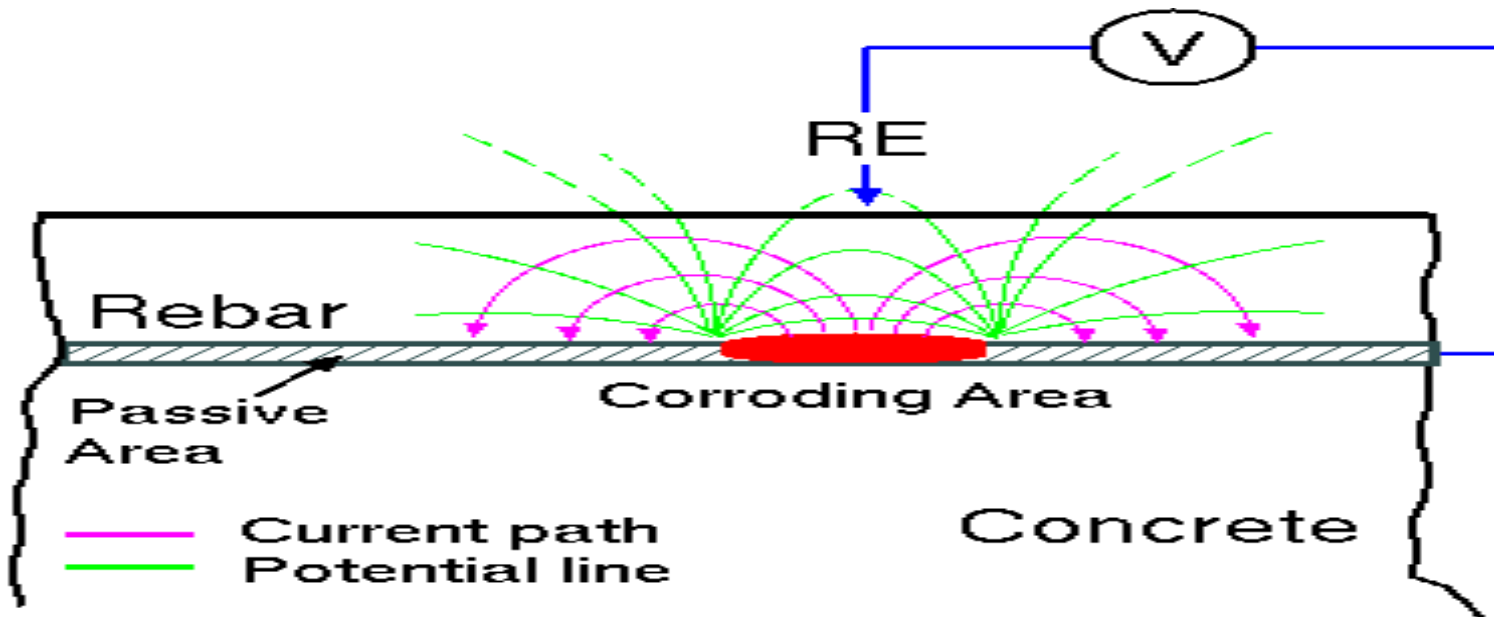
- Potential Mapping
- Concrete Resistivity



Kampung. Jawa, Banda Aceh



# Limitation of Direct Analysis



## Potential Mapping Method

- Less Accurate
- Laborious
- Time Consuming

**Important !**

**Effective NDE Method**

# PROPOSED METHOD:

**INVERSE ANALYSIS**

**BOUNDARY ELEMENT  
METHOD**

**PARTICLE SWARM  
OPTIMIZATION**

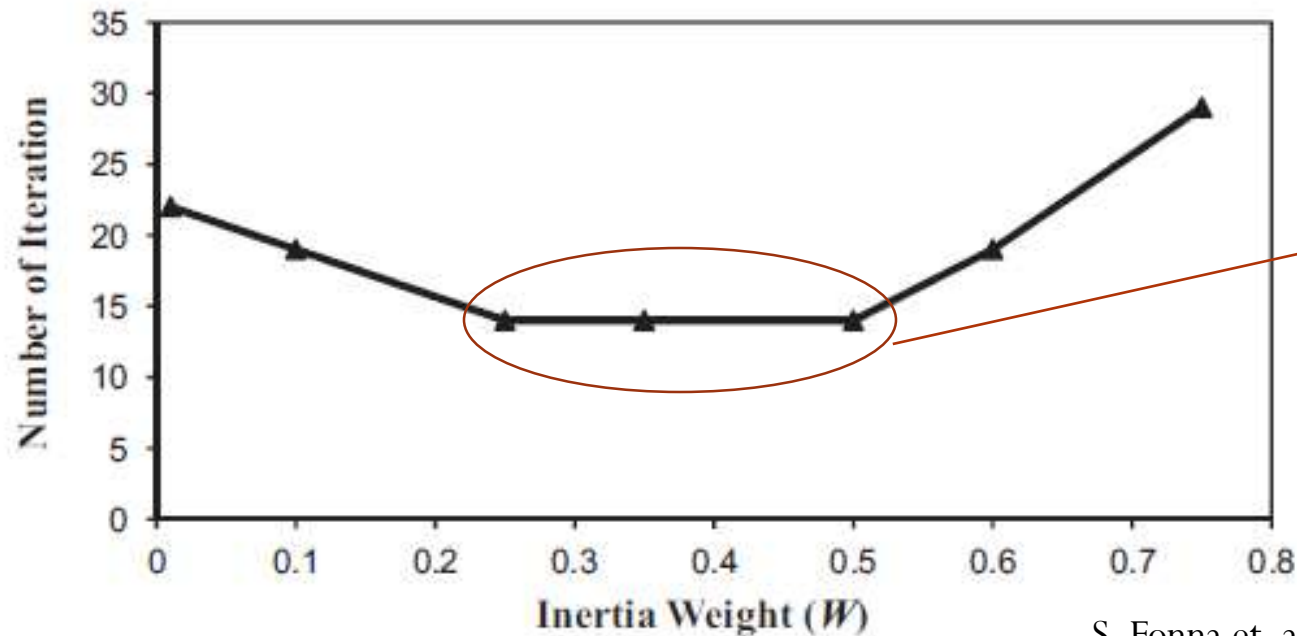


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graph TD; A[BOUNDARY ELEMENT METHOD] --> C[BOUNDARY ELEMENT INVERSE ANALYSIS (BEIA)]; B[PARTICLE SWARM OPTIMIZATION] --> C;
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**BOUNDARY ELEMENT  
INVERSE ANALYSIS (BEIA)**

S. Fonna et. al. 2013

## Previous study



S. Fonna et. al. 2013

Parsopoulos and Vrahatis (2010) suggested to use inconstant  $W$  for better result

The purpose of this study:

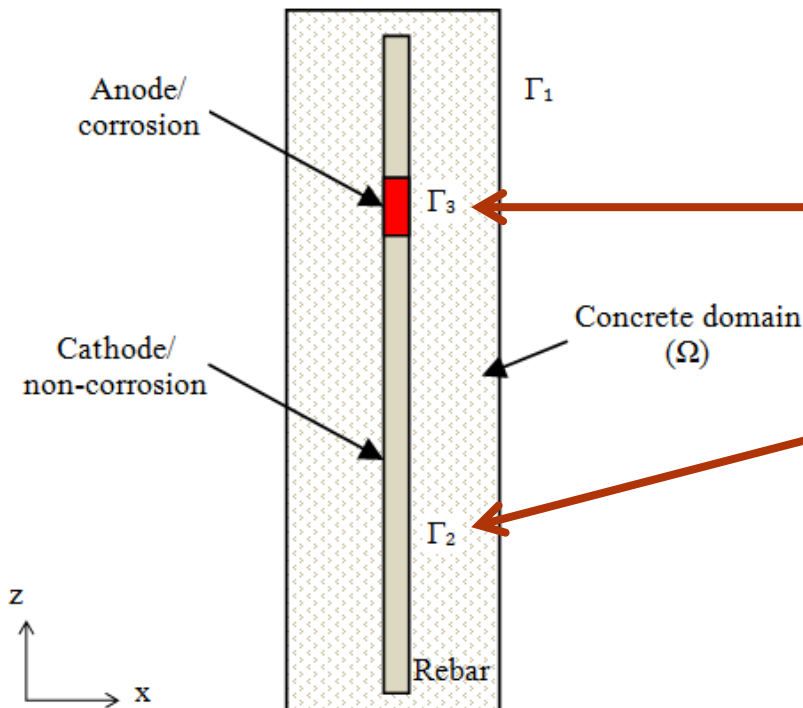
To investigate the effect of inconstant  $W$  (with  $W_{up} = 0.5$  and  $W_{low} \leq 0.5$ ) on the performance of BEIA in detecting rebar corrosion in concrete

# Modeling of Corrosion Problems

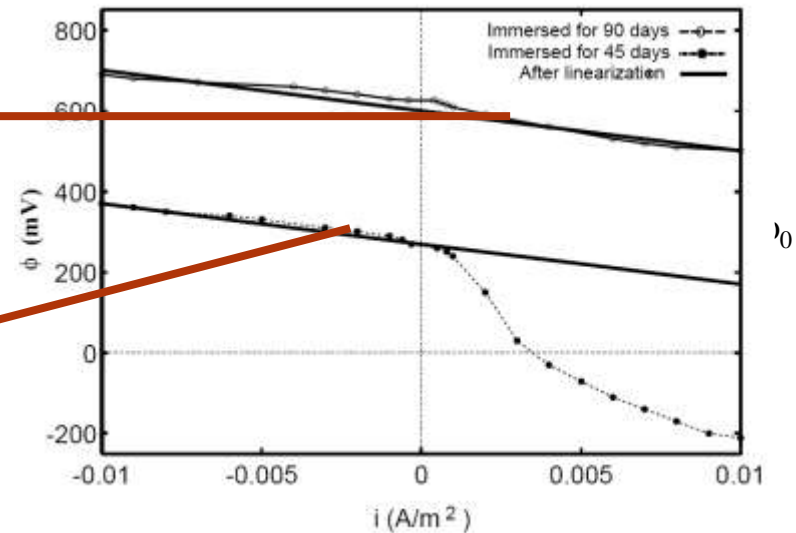
Laplace's Equation

$$\nabla^2 \phi = \frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = 0 \quad \text{In } \Omega$$

Boundary conditions:



Polarization curve:



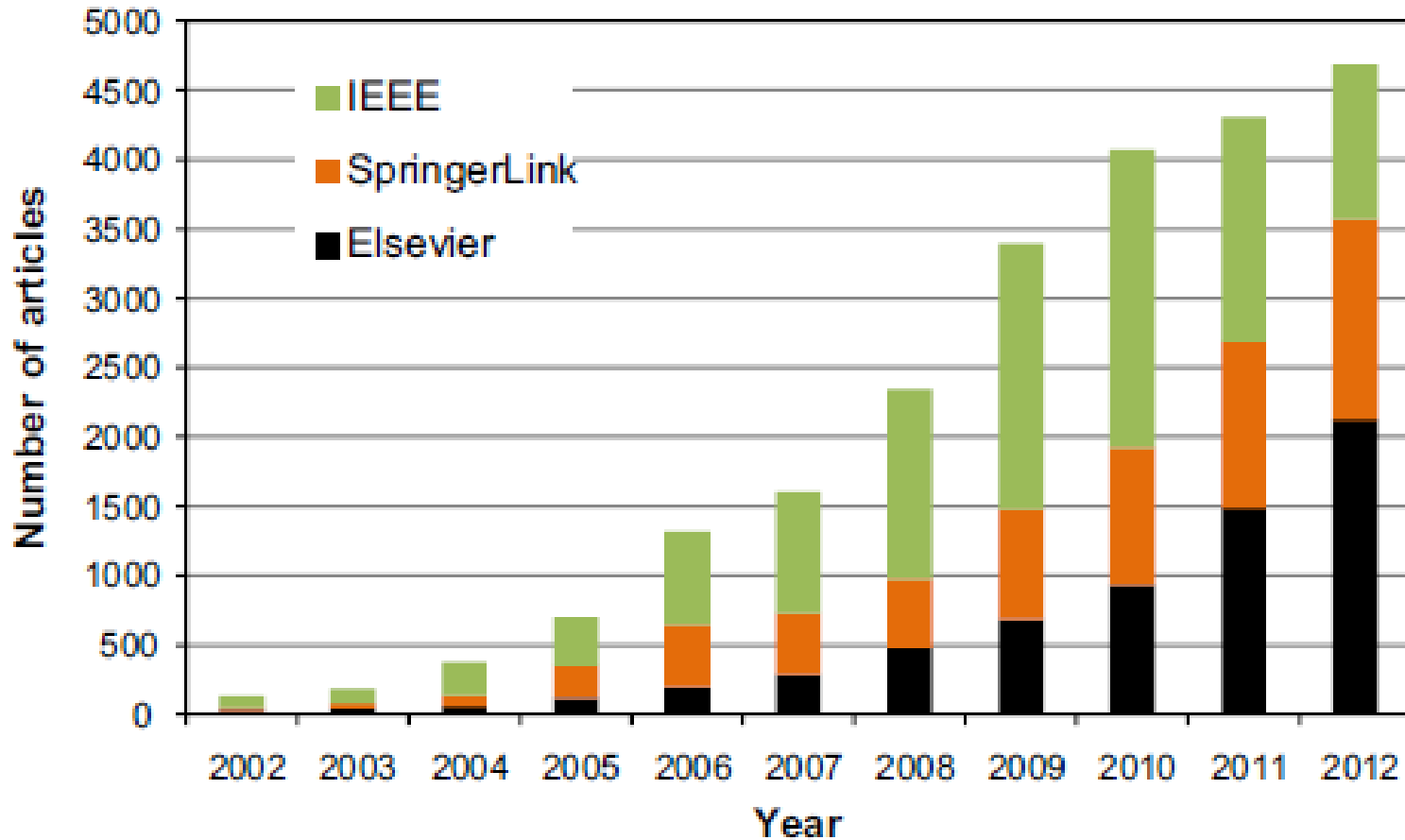
Ridha et al. 2005

BEM: Solving the Laplace's Eq.

Obtain:  $\phi$  and  $i$  in the whole  $\Omega$



# WHY PSO ???



S. Fonna et. al. 2013

- Simple algorithm
- Comparable accuracy

# Particle Swarm Optimization

- ❑ Introduced by Kennedy and Eberhart in 1995
- ❑ Population-based search algorithm
- ❑ Inspired by flocking behavior of birds

## Pseudocode of PSO

Input:	Number of particle ( $Z$ ), Swarm ( $S$ ), best position ( $P$ )
Step 1.	<b>Set</b> $j \leftarrow 1$
Step 2.	<b>Initialize</b> $S$ and <b>Set</b> $P \equiv S$ Calculate $W$ using Eq. c
Step 3.	<b>Evaluate</b> $S$ and $P$ , and define index $g$ of the best position
Step 4.	<b>While</b> (termination criterion not met)
Step 5.	<b>Update</b> $S$ using Eq. a and b
Step 6.	<b>Evaluate</b> $S$
Step 7.	<b>Update</b> $P$ and redefine index $g$
Step 8.	<b>Set</b> $j \leftarrow j + 1$
Step 9.	<b>End While</b>
Step 10.	<b>Print</b> best position found

$$X_{j+1} = X_j + V_{j+1} \quad (a)$$

$$V_{j+1} = W_j V_j + a_1 r_1 (pbest - X_j) + a_2 r_2 (gbest - X_j) \quad (b)$$

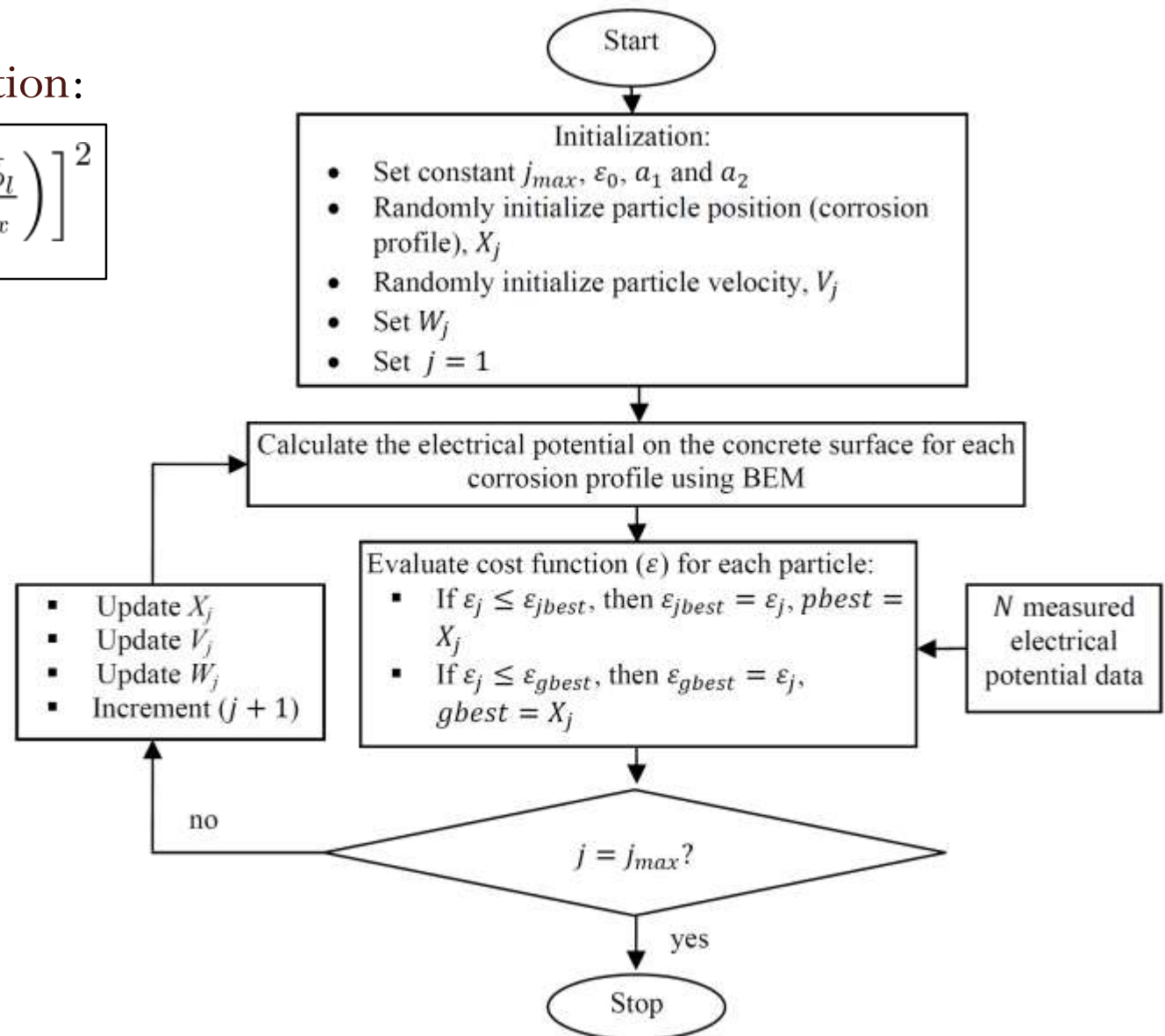
$$W_j = W_{up} - \left[ (W_{up} - W_{low}) \frac{j}{j_{max}} \right] \quad (c)$$

# Boundary Element Inverse Analysis

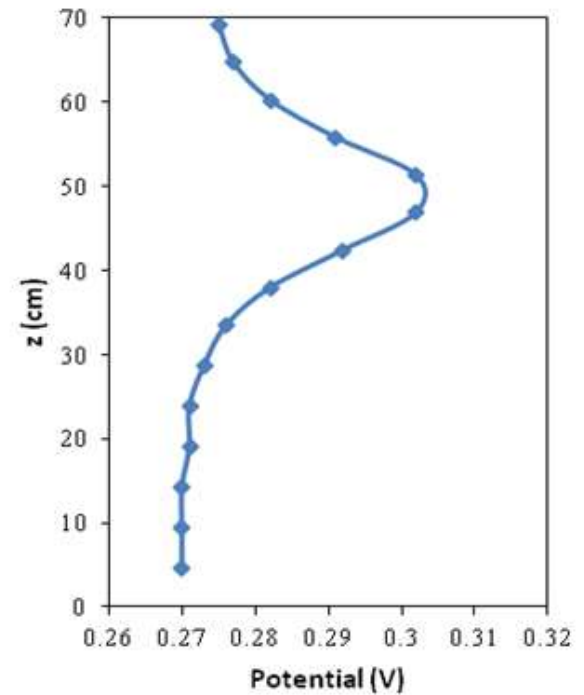
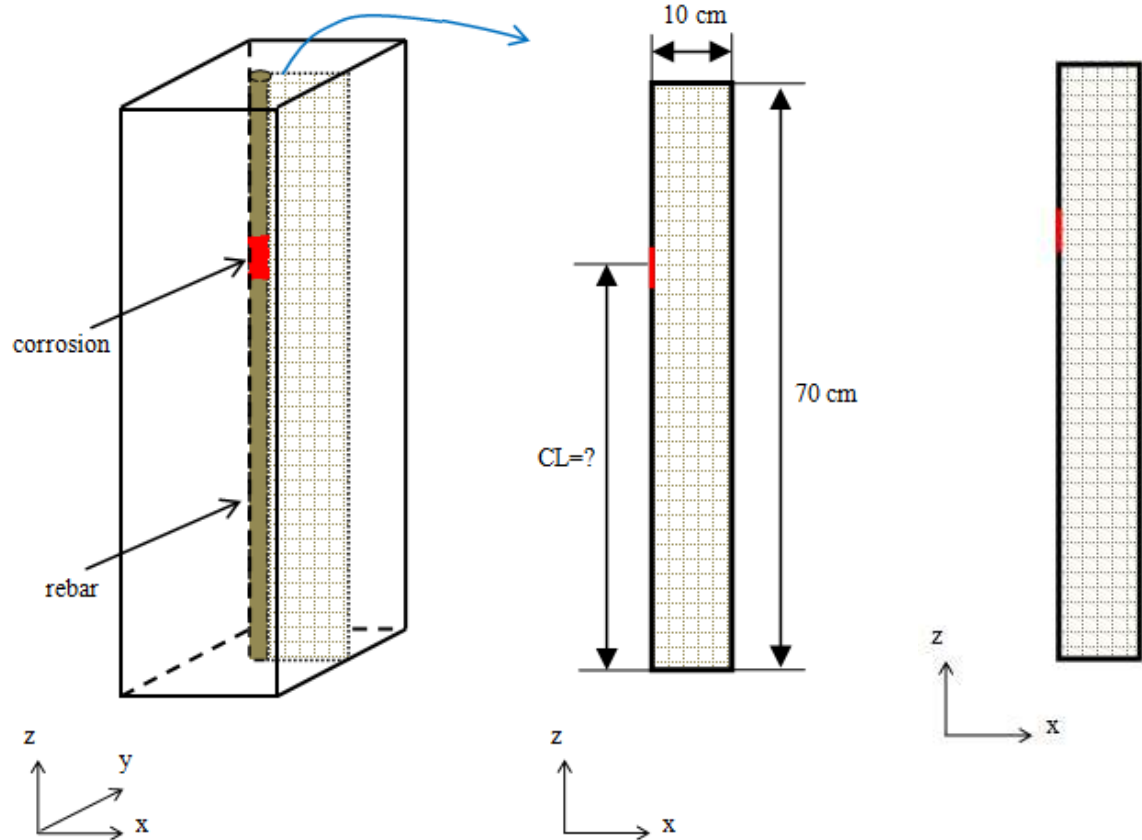
The flowchart of inverse analysis using PSO

Minimize cost function:

$$\varepsilon(C) = \sum_{l=1}^N \left[ \left( \frac{\phi_l - \bar{\phi}_l}{\phi_{max}} \right) \right]^2$$



# Numerical Simulation Setup, Results and Discussion



$\kappa = 0,007 \Omega^{-1}\text{m}^{-1}$ ;  $\epsilon_0 \leq 10^{-4}$ ;  $a_1 = a_2 = 0.5$ ;  
and  $N = 15$

Constant parameters

$$\phi_a = 0.600 - 10i \quad (\text{V})$$

$$\phi_c = 0.270 - 10i \quad (\text{V})$$

Generated from the polarization curves

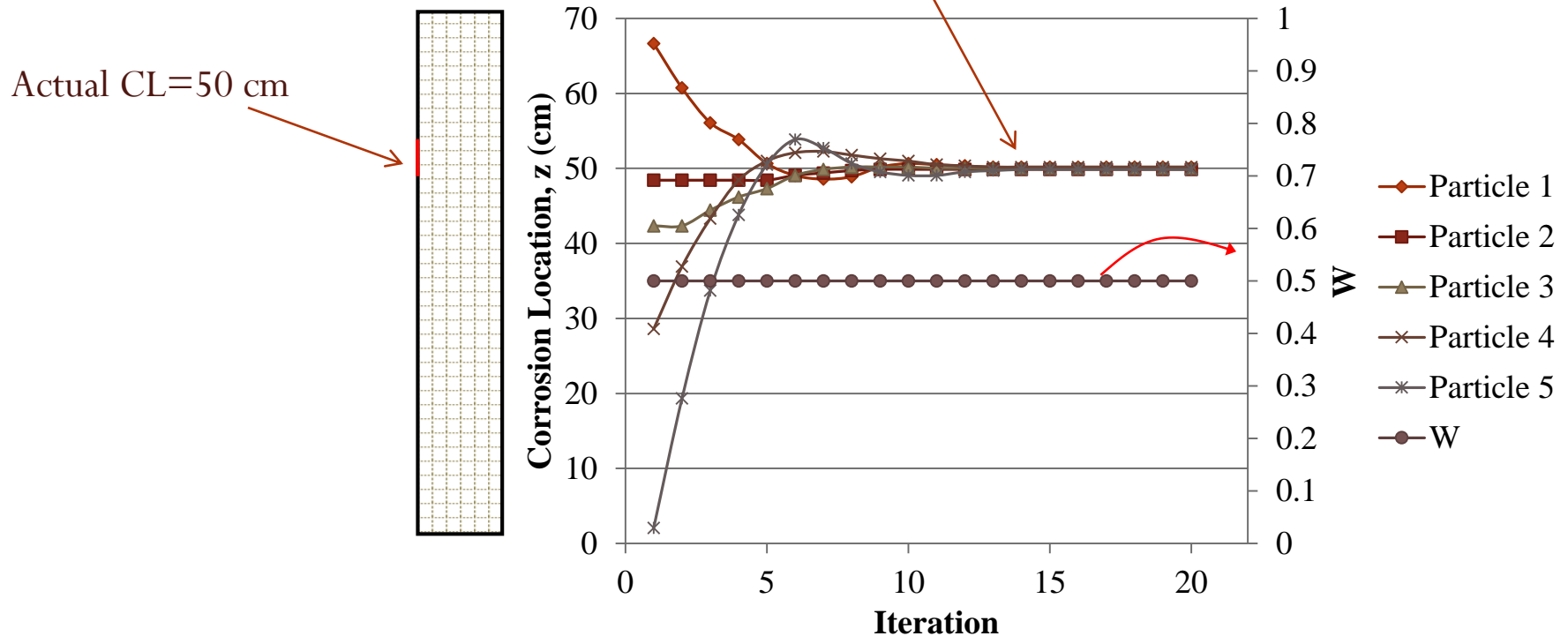
BEM simulation result with corrosion location at  $x=50$  cm and size 2 cm

The values of  $W_{up}$  and  $W_{low}$  for the simulation

No.	$W_{up}$	$W_{low}$	Gradient of $W$ during iteration
1	0.5	0.5	0
2	0.5	0.2	-0.015
3	0.5	0.01	-0.0245

## Simulation no. 1

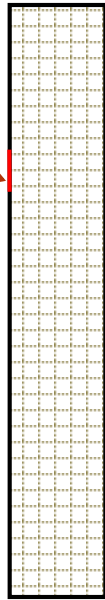
CL obtain on iteration 14<sup>th</sup>  
with Error=0.26%



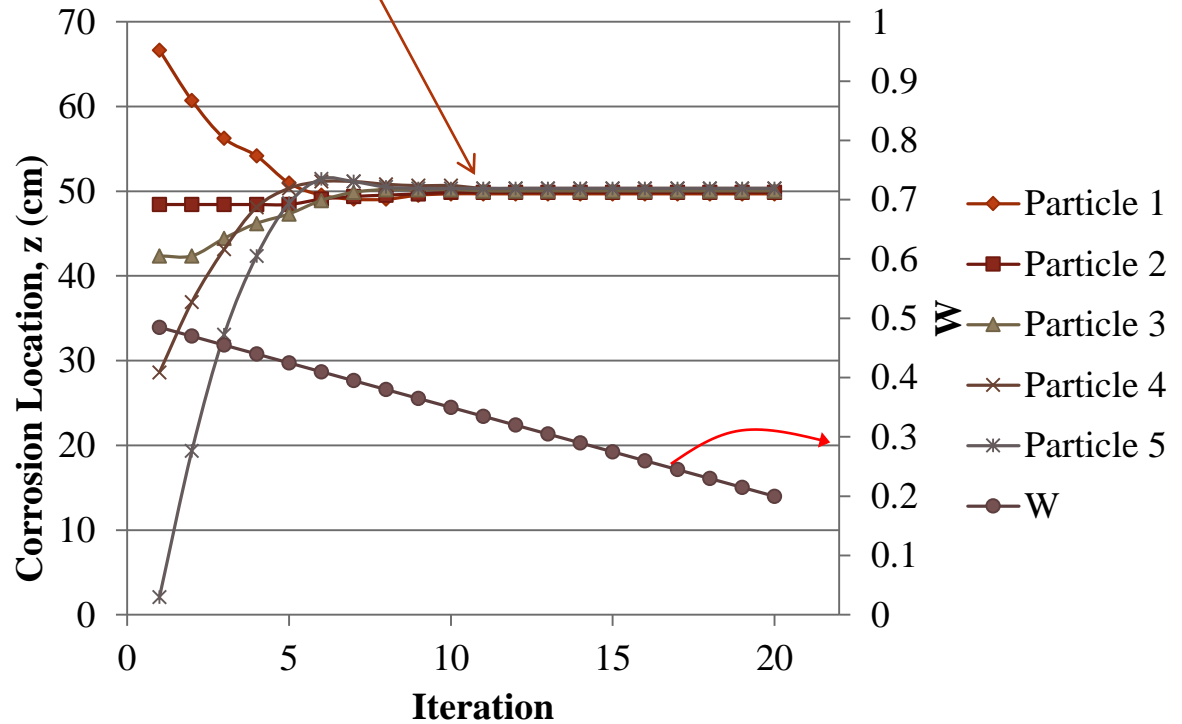
The particle movement and the value of  $W$  during iteration for  $W_{up} = 0.5$  and  $W_{low} = 0.5$

# Simulation No. 2

Actual CL=50 cm



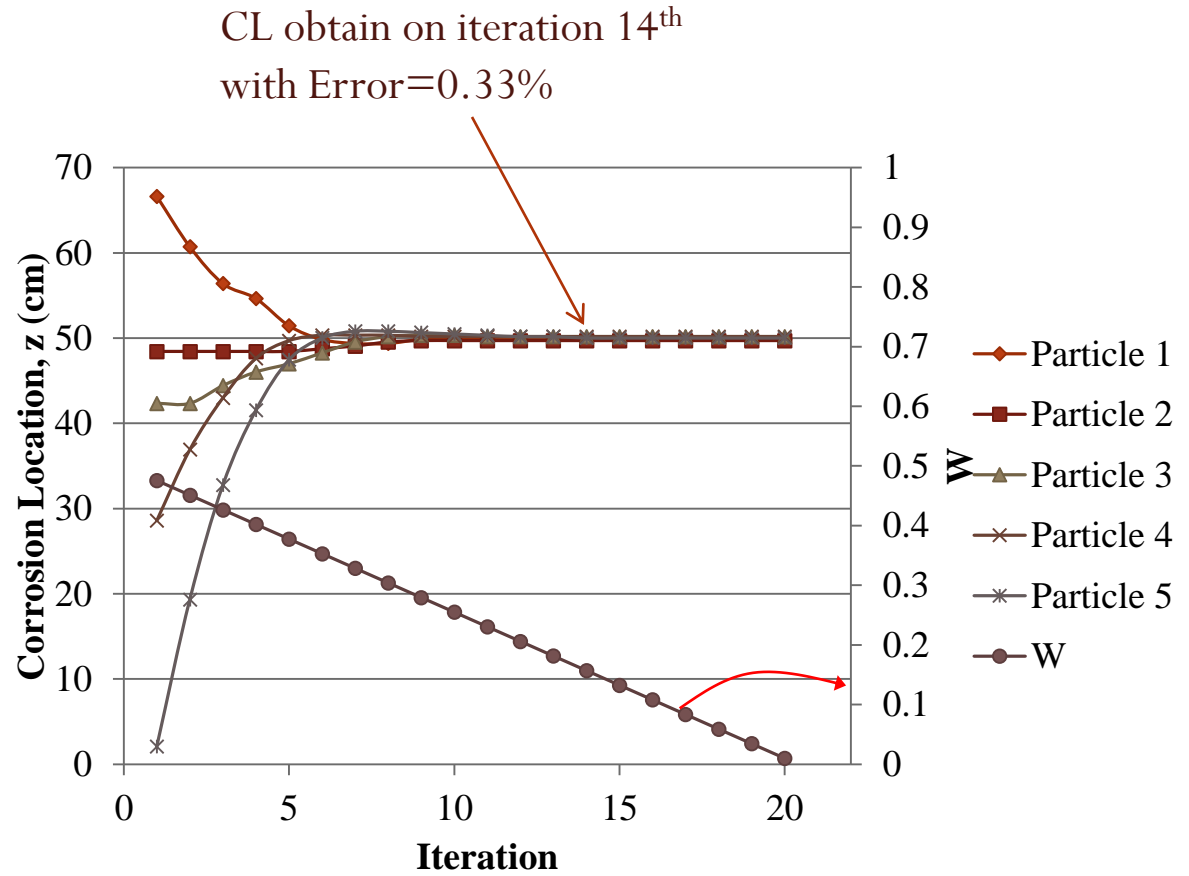
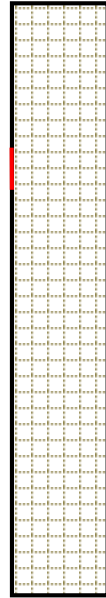
CL obtain on iteration 11<sup>th</sup>  
with Error=0.46%



The movement of particles and value of  $W$  during iteration for  $W_{up} = 0.5$  and  $W_{low} = 0.2$

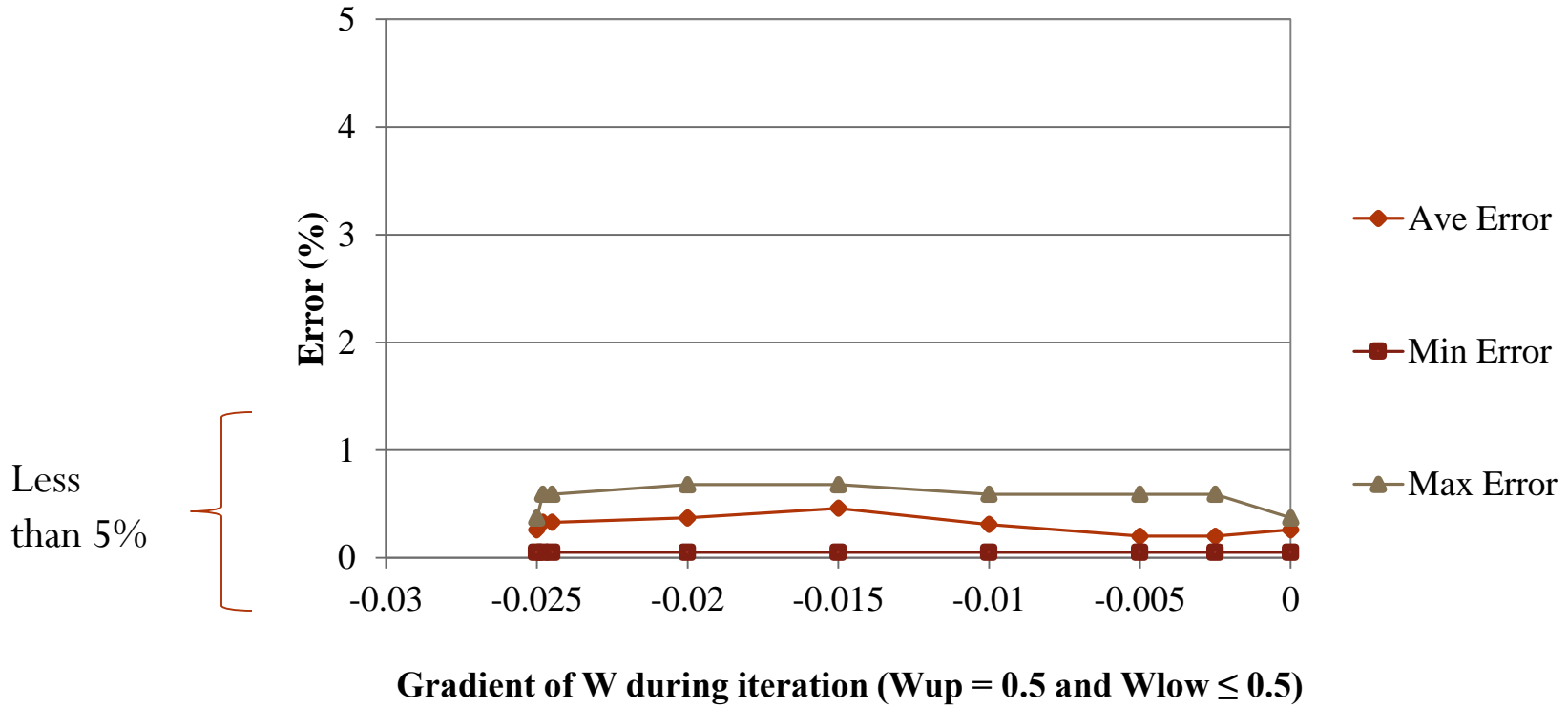
# Simulation No. 3

Actual CL=50 cm



The movement of particles and value of  $W$  during iteration for  $W_{up} = 0.5$  and  $W_{low} = 0.01$

# Resume of all simulation



The error in detecting actual corrosion for  $W_{up} = 0.5$  and  $W_{low} \leq 0.5$



# Conclusions

- The effect of inconstant  $W$  on BEIA when detecting rebar corrosion in concrete was explored
- the inconstant  $W$  with  $W_{up} = 0.5$  and  $W_{low} \leq 0.5$  did not influence the performance of the BEIA in detecting rebar corrosion
- The error with respect to the actual location of corrosion (inconstant  $W$  with  $W_{up} = 0.5$  and  $W_{low} \leq 0.5$ ) was less than 5%

## **Further study:**

important to conduct further research to study the effect of  $W_{up} > 0.5$  for inconstant  $W$

THANK YOU